

# Bias in Arctic Ocean SST Retrieval from Metop-A AVHRR

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# Introduction

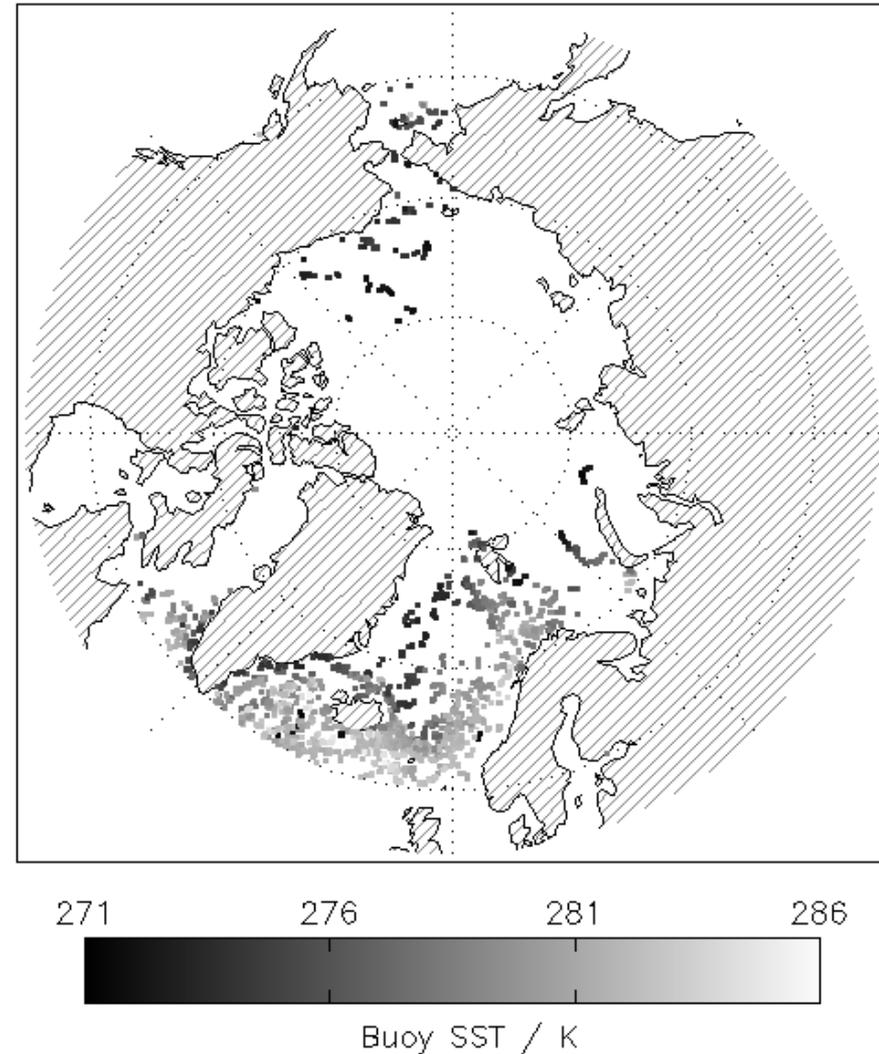
- Perception that SST retrieval biases are poor in Arctic
- Retrieval informed by simulations helps reduce biases from atypical atmospheric profiles
- But biases may arise in simulations from
  - forward model errors
  - biases in NWP used for simulations
  - sensor calibration
- Moreover, the error covariance of simulations is not well known

# Aims

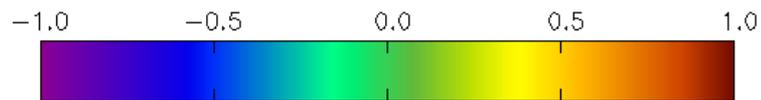
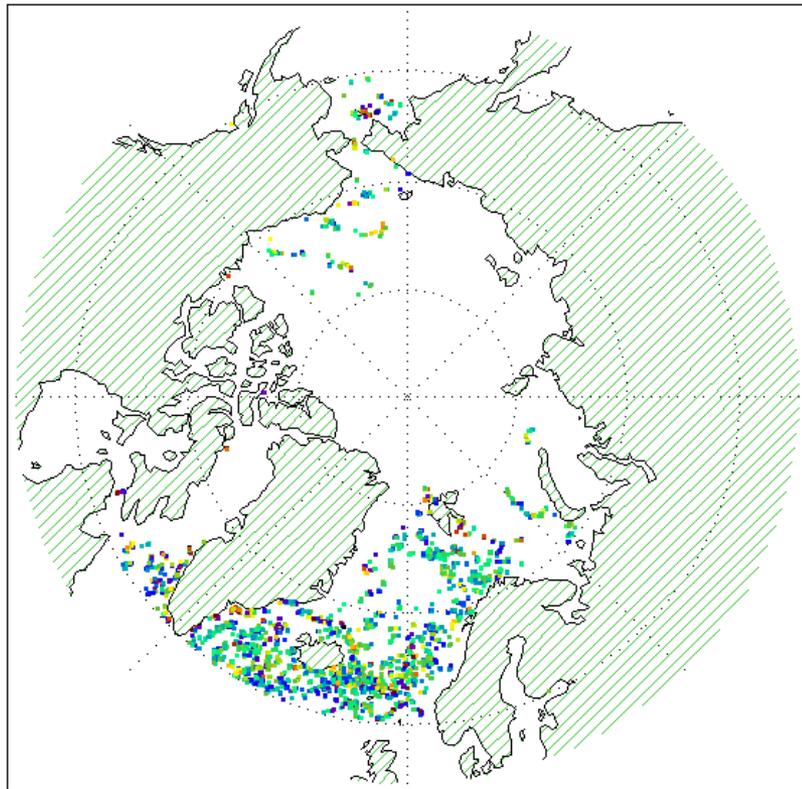
- Assess significance of biases vs drifters
  - OSTIA
  - operational 3-channel SST retrieval coefficients
    - ditto plus simulated SST bias correction
  - naïve implementation of optimal estimation
    - with and without SAF BT bias adjustment
- Consider two candidate “bias tolerant” approaches to retrieval
  - can we design the retrieval such that the BT bias adjustment is unnecessary

# Data

- Match-up dataset from SAF
- Metop-A AVHRR
- 1 year of data, filtered against buoy blacklist
- Solar zenith angles  $> 90$  deg (twilight and night)
- 3.7, 11 and 12  $\mu\text{m}$  BT,  $\text{dBT}/\text{dx}$ ,  $\text{dBT}/\text{dw}$
- CLs, angles, OSTIA, lat etc
- 4383 matches only



# OSTIA vs Drifters



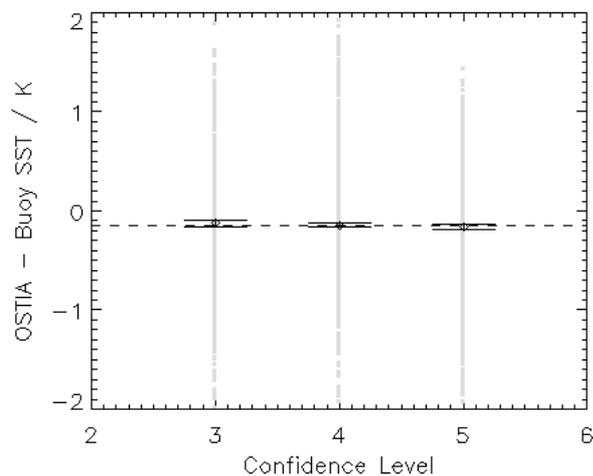
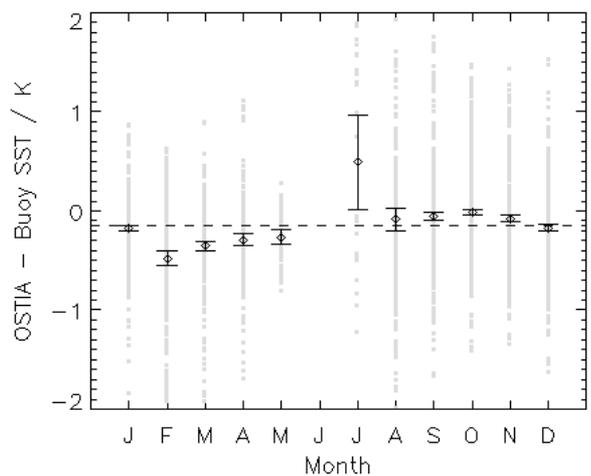
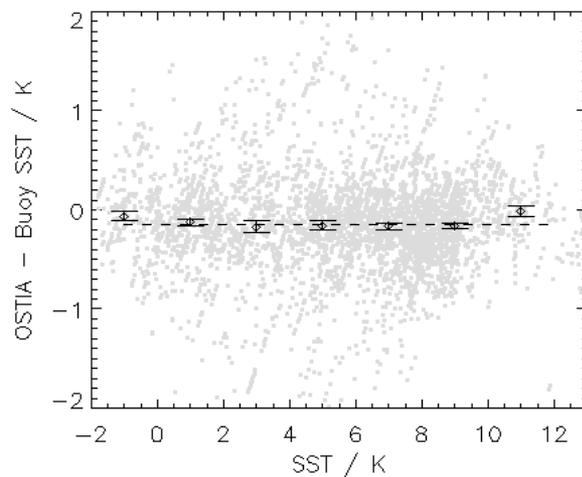
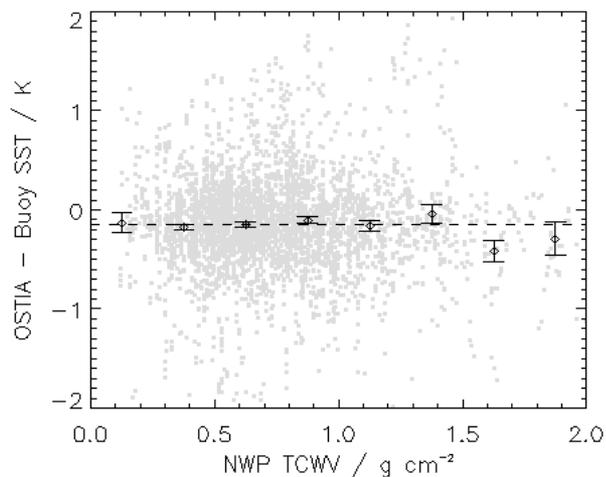
OSTIA - Buoy SST / K

Note: not an independent comparison

Mean:  $-0.14 \pm$  SD 0.51 K

Median:  $-0.14 \pm$  RSD 0.34 K

# OSTIA vs Drifter



Diamond:  
mean difference  
in bin

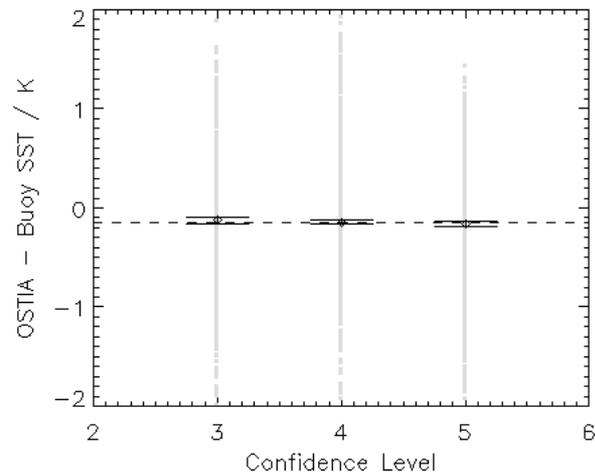
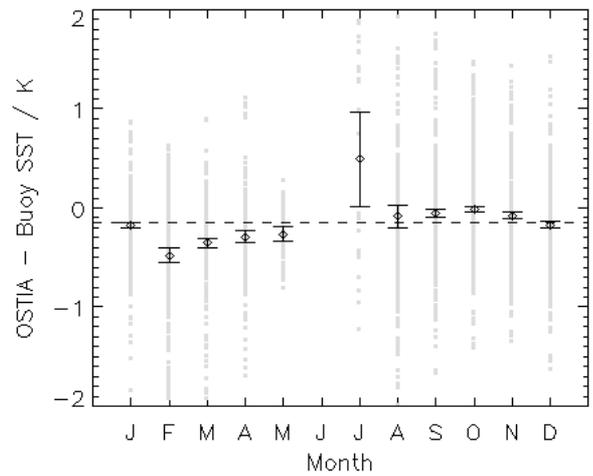
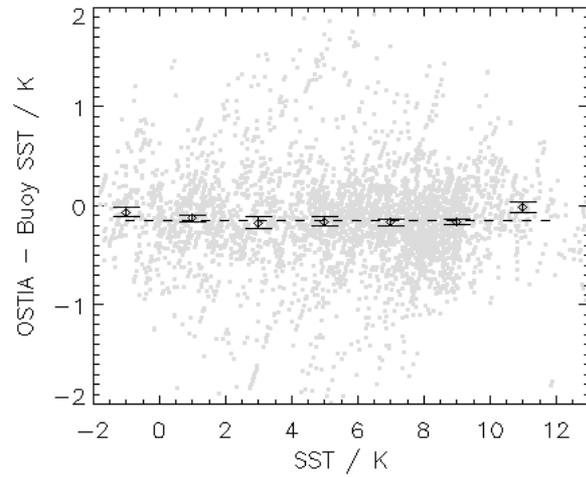
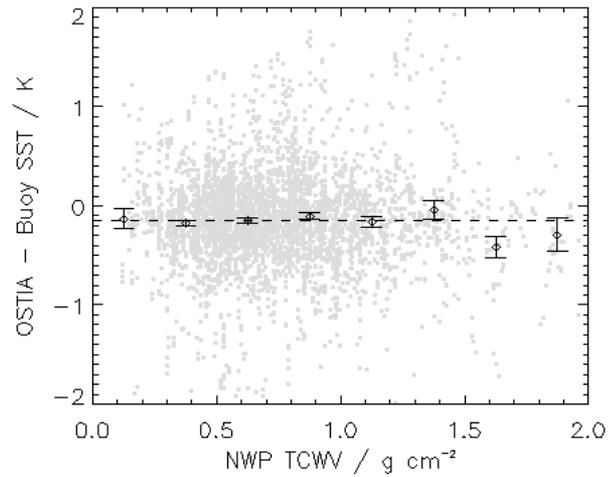
Bar:  
95% confidence  
interval on the  
mean difference

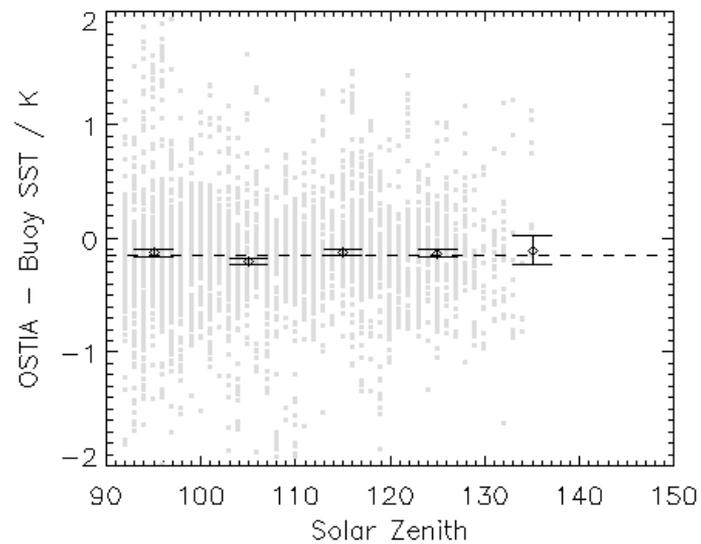
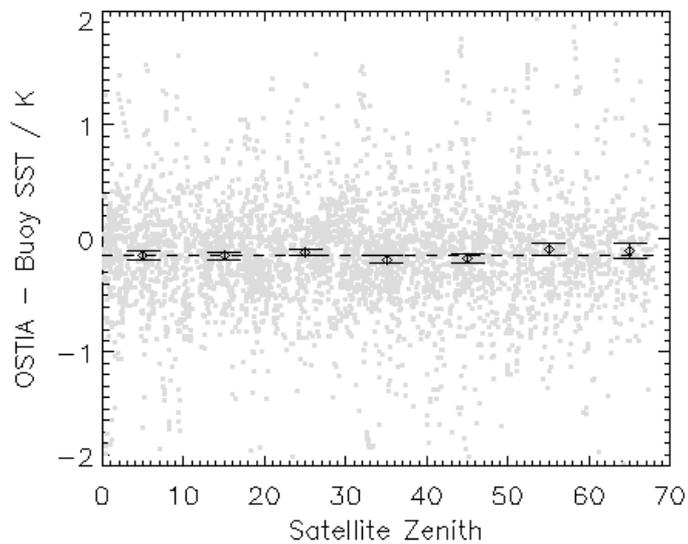
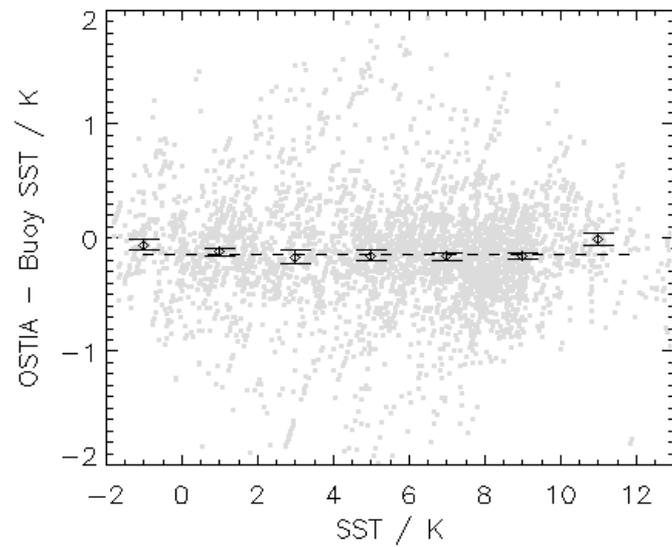
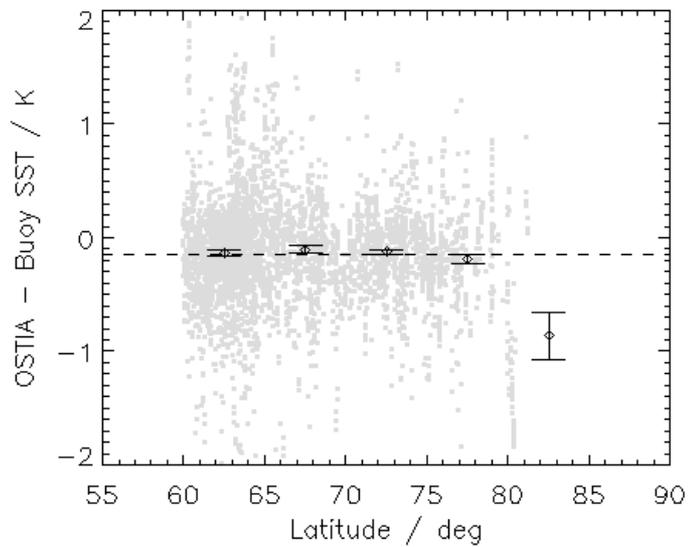
Dashed line:  
Overall mean  
difference

# Interpretation of the confidence interval

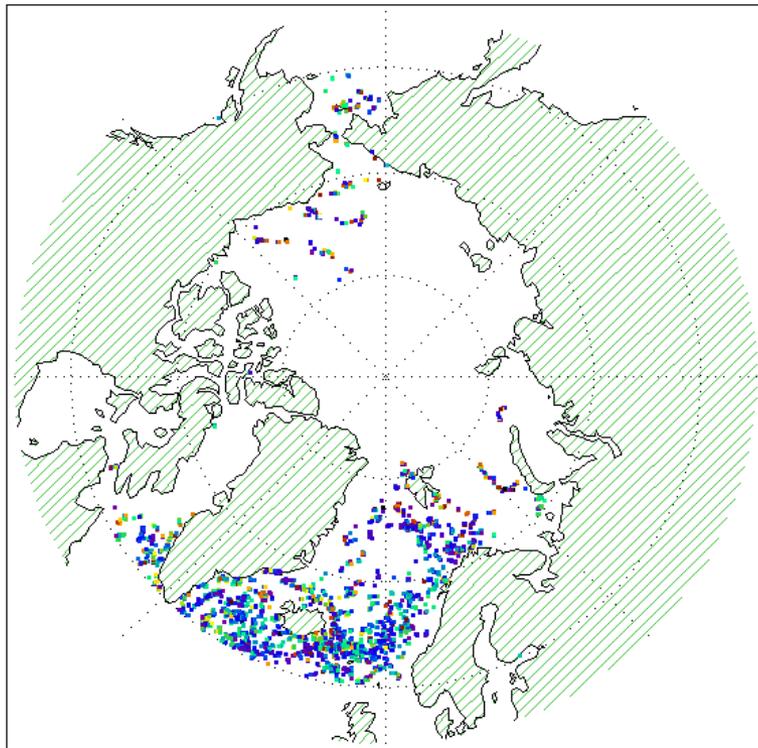
- How the CI was calculated
  - mean +/- t-factor \* ( standard deviation/sqrt(n-1) )
  - for large n, t-factor  $\rightarrow$  1.96 (i.e., ~"two sigma")
  - for n = 3, t-factor  $\sim$  4
- Assumption is independent errors
- But buoy contribution to difference is probably correlated for each buoy ID, so CIs are still underestimated
- Can't confidently say bias exists if bar overlaps

# OSTIA vs Drifter





# Operational Triple Coefficients



-1.0      -0.5      0.0      0.5      1.0



Op SST - Buoy SST / K

Mean:  $-0.55 \pm$  SD 0.60 K (4383)

Median:  $-0.53 \pm$  RSD 0.42 K

CL = 5

Mean:  $-0.52 \pm$  SD 0.48 K (1629)

Median:  $-0.52 \pm$  RSD 0.39 K

CL = 4

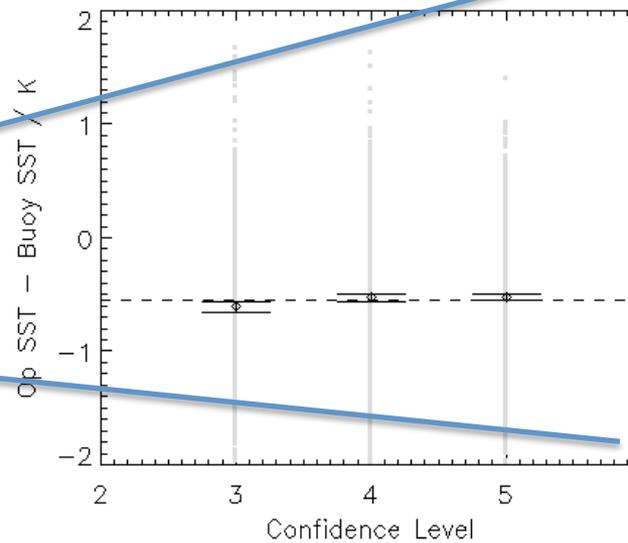
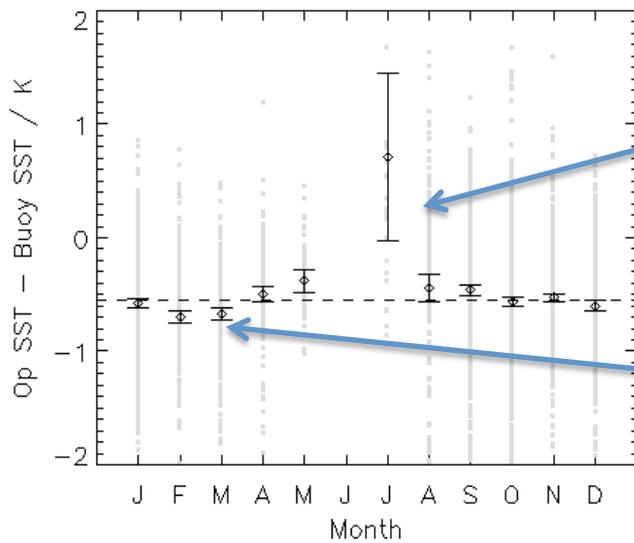
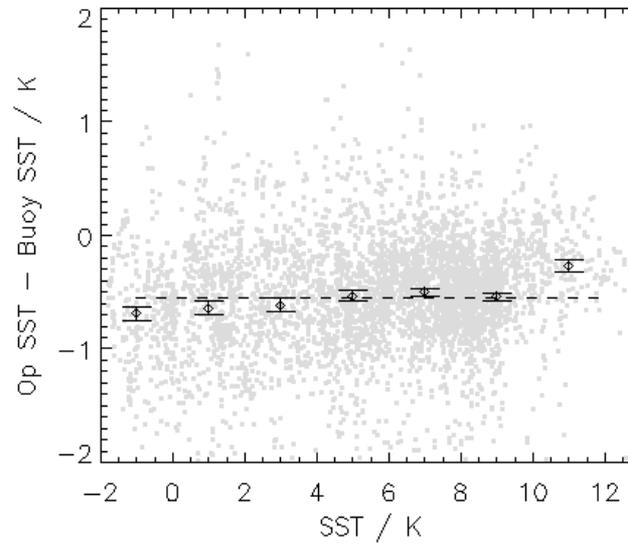
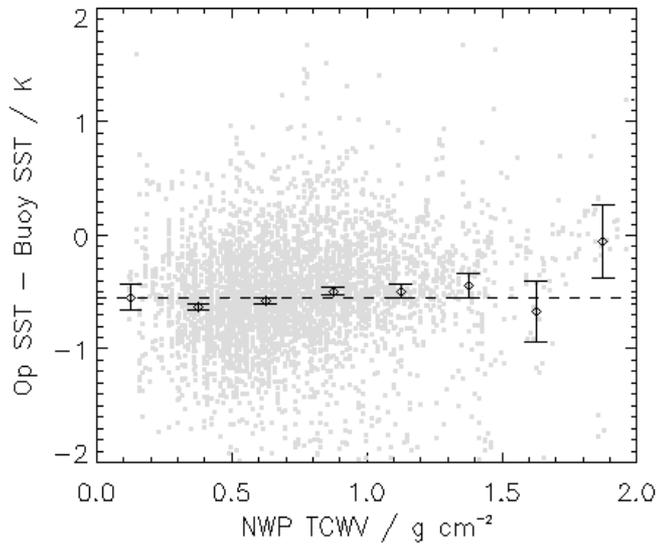
Mean:  $-0.53 \pm$  SD 0.59 K (1710)

Median:  $-0.50 \pm$  RSD 0.39 K

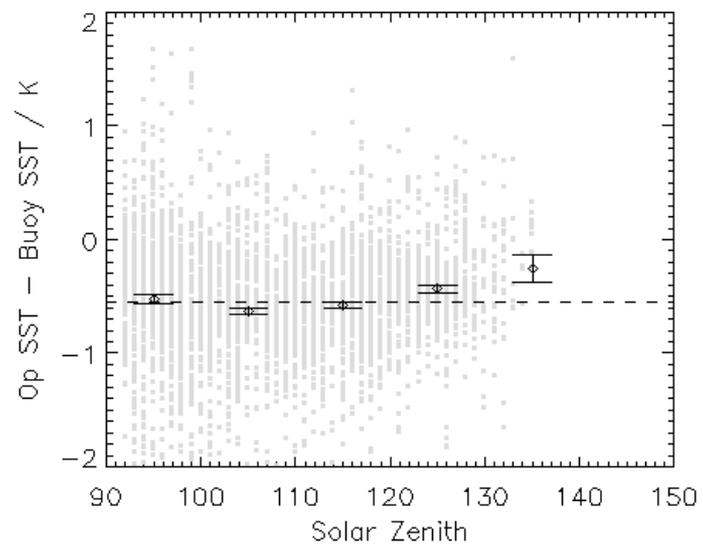
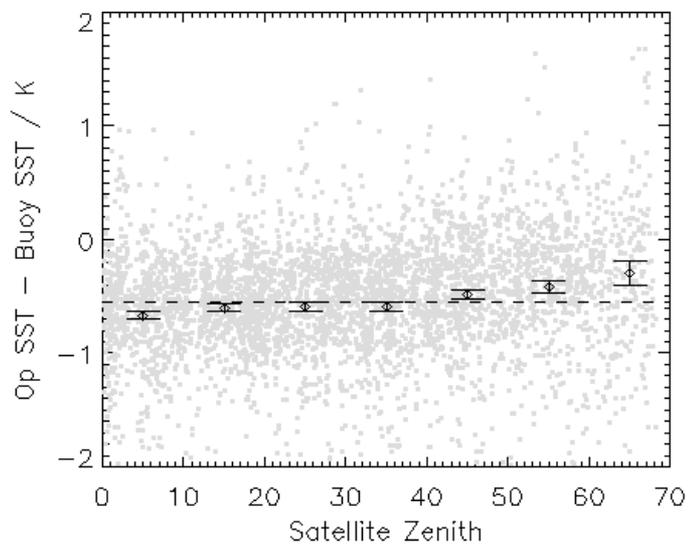
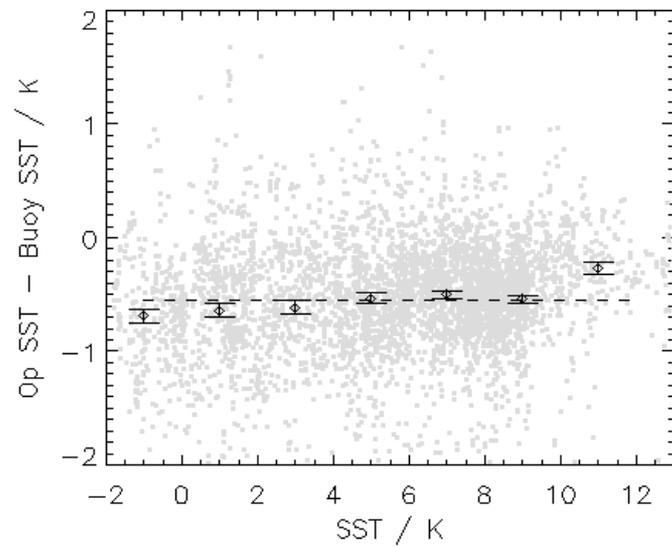
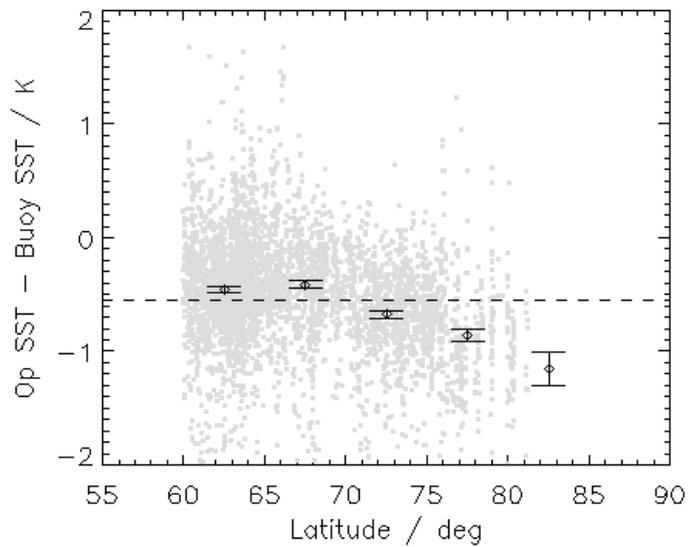
CL = 3

Mean:  $-0.61 \pm$  SD 0.76 K (1044)

Median:  $-0.61 \pm$  RSD 0.52 K

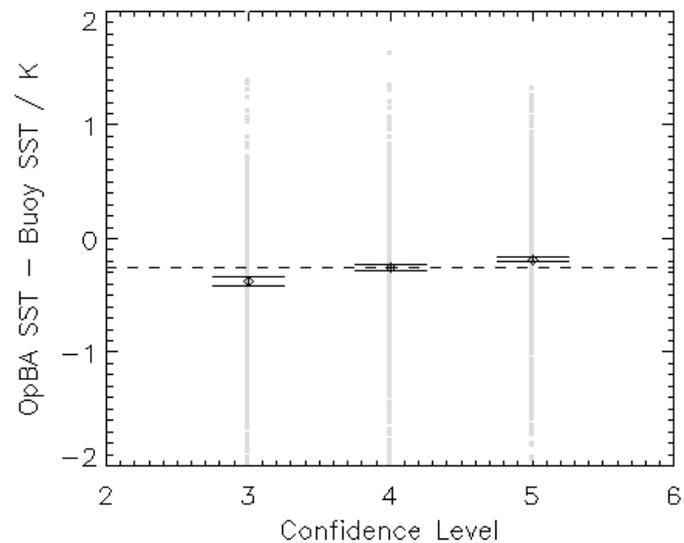
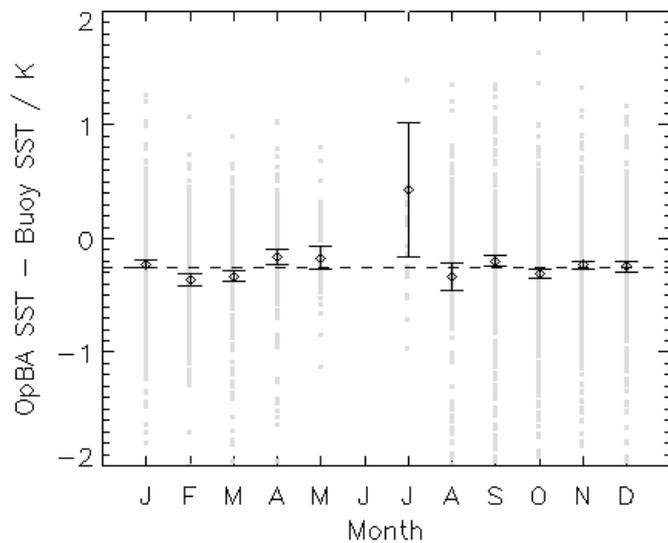
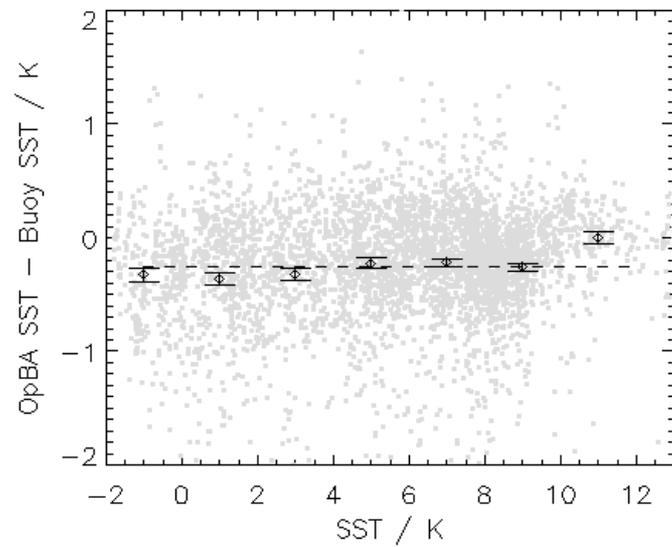
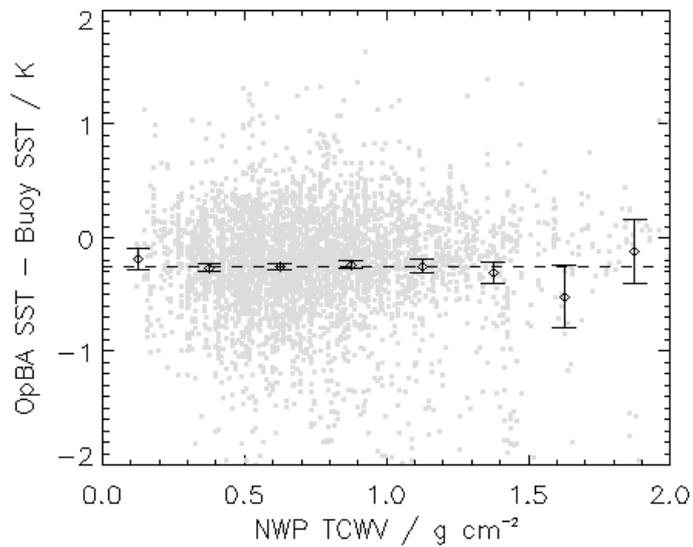


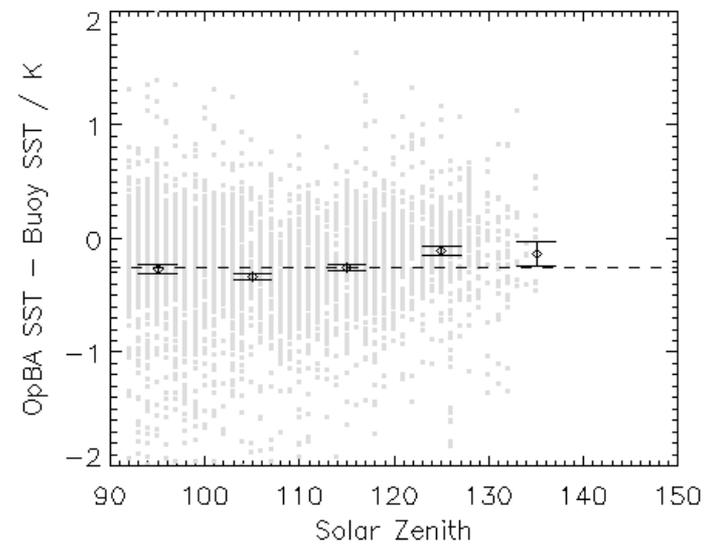
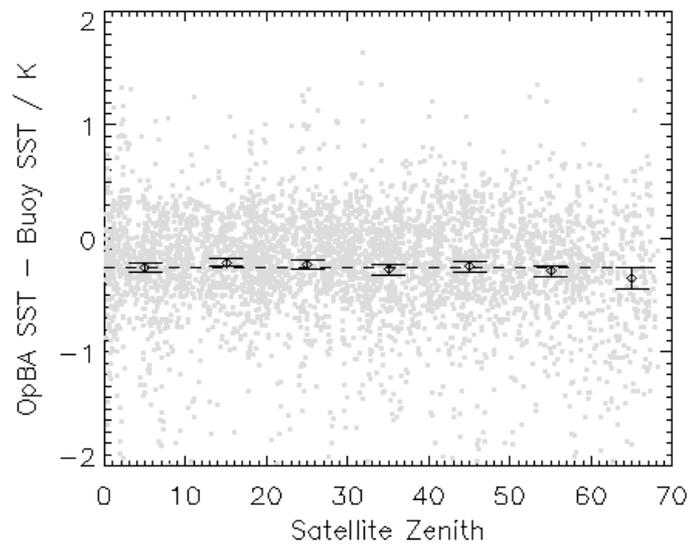
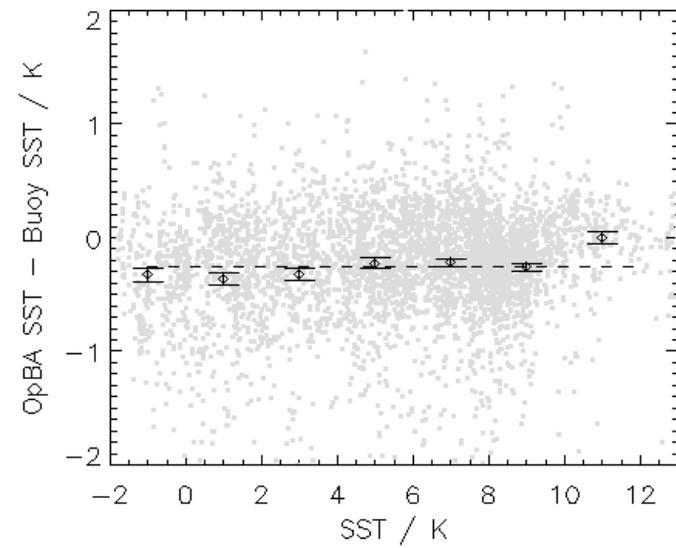
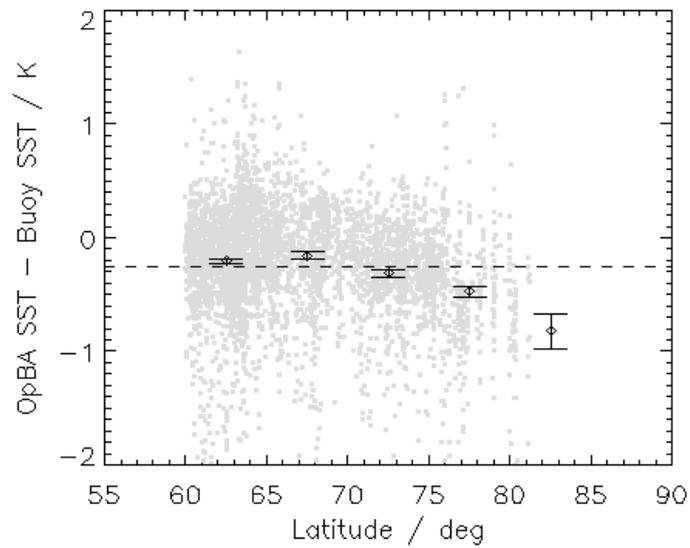
Speculation:  
 Influenced by real near-surface stratification between buoy and skin? Or a twilight effect?  
 Strong winter skin effect in satellite obs?



# Simulated Bias Correction

- Put the RTTOV-simulated BTs through the same retrieval coefficients
- Subtract the simulated retrieved bias (known given that we know the SST that went into the simulations)





# Op with Sim Bias Correction

- Mean:  $-0.26 \pm \text{SD } 0.57 \text{ K}$  (4383)
- Median:  $-0.21 \pm \text{RSD } 0.39 \text{ K}$
- Question: are these coefficients intended to deliver skin or subskin SST? (Is the  $T_{\text{corr}}$  coefficient tuned to buoys or buoys –  $0.17 \text{ K}$ ?)
- If subskin, there is an overall bias still
- If skin, bias is  $<0.1 \text{ K}$

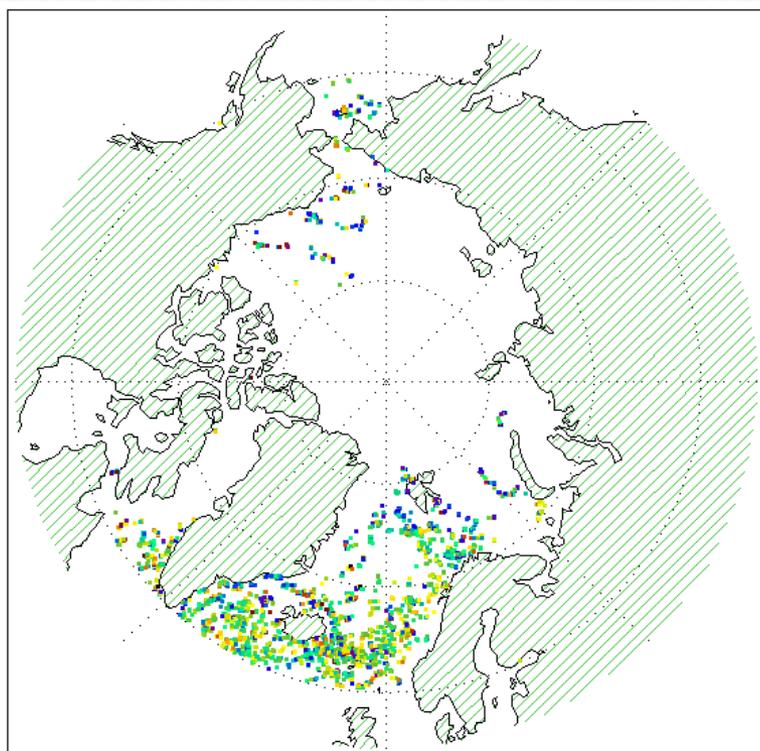
# Optimal Estimation (MAP)

- OE assumes
  - zero bias in simulation relative to observation
  - we have good estimates of the prior error covariance ( $S_a$ )
  - we have good estimates of the sensor noise and forward model error covariance ( $S_e$ )
- All are not true, and the first in particular prompts BT bias adjustment efforts

# Naïve OE implementation

- Assume zero S-O bias, don't use SAF BT bias adjustments
- $e_{xb} = 1.0$  K
- $e_{wb} =$  as recent SEVIRI paper
- $e_y = 0.1$  K (same noise all channels)
- $e_F = 0.15$  K (RTTOV error independent between channels)
- Skin SST retrieval, then add 0.17 K to cf. drifters

# OE (MAP no BC) vs drifters



-1.0      -0.5      0.0      0.5      1.0



MAP SST - Buoy SST / K

MAP, no SAF bias correction

CL = 5

Mean: -0.01 +/- SD 0.48 K (1629)

Median: 0.04 +/- RSD 0.38 K

CL = 4

Mean: -0.06 +/- SD 0.59 K (1710)

Median: 0.01 +/- RSD 0.37 K

CL = 3

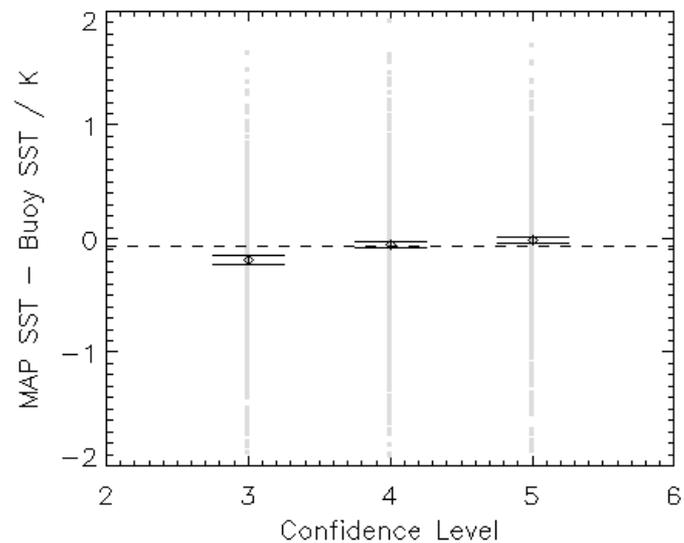
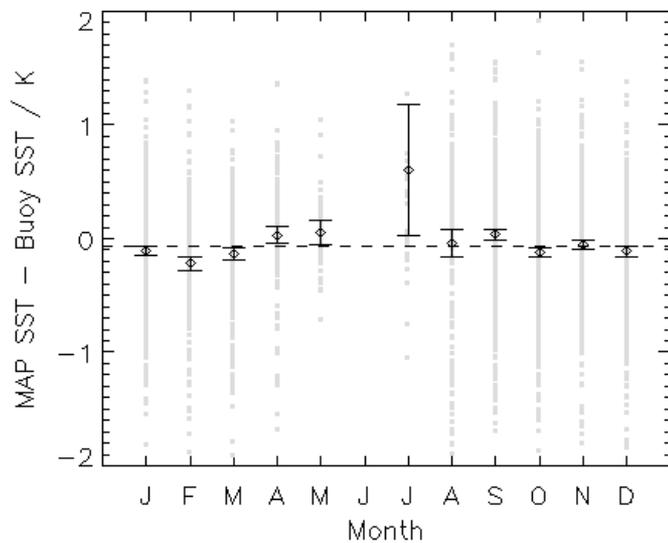
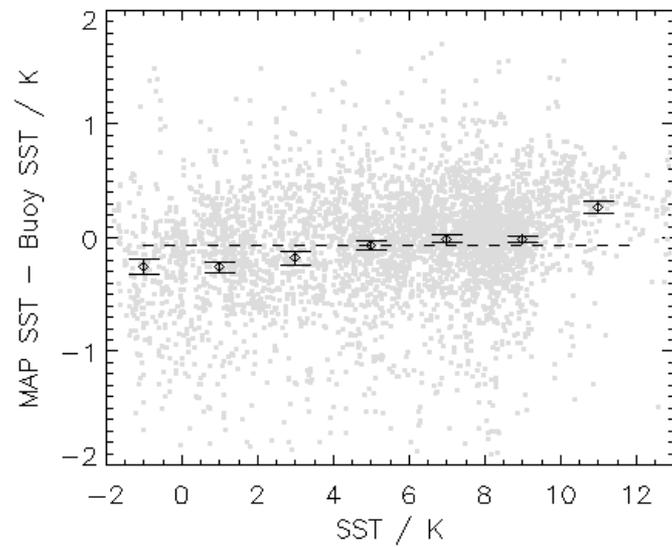
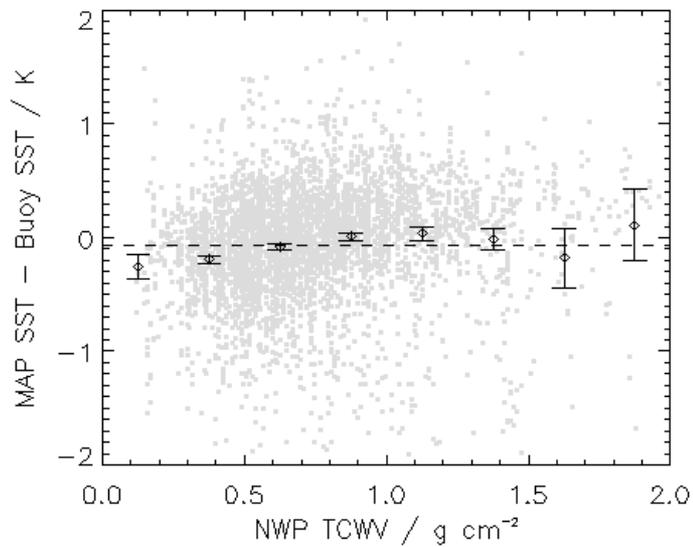
Mean: -0.19 +/- SD 0.68 K (1044)

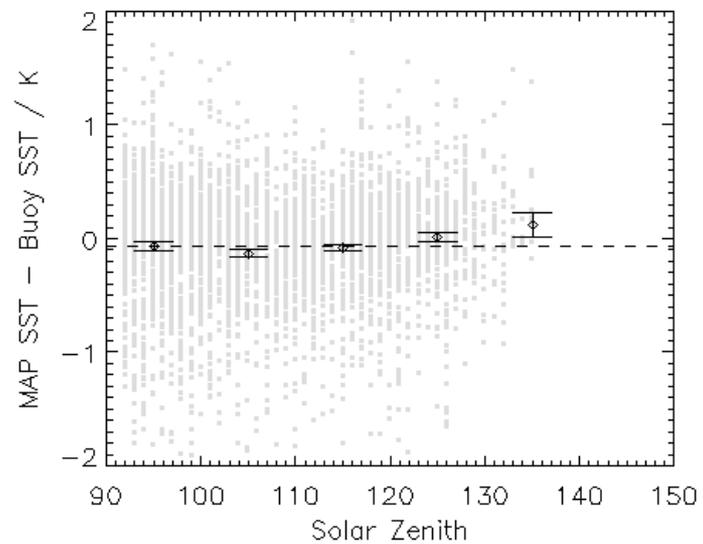
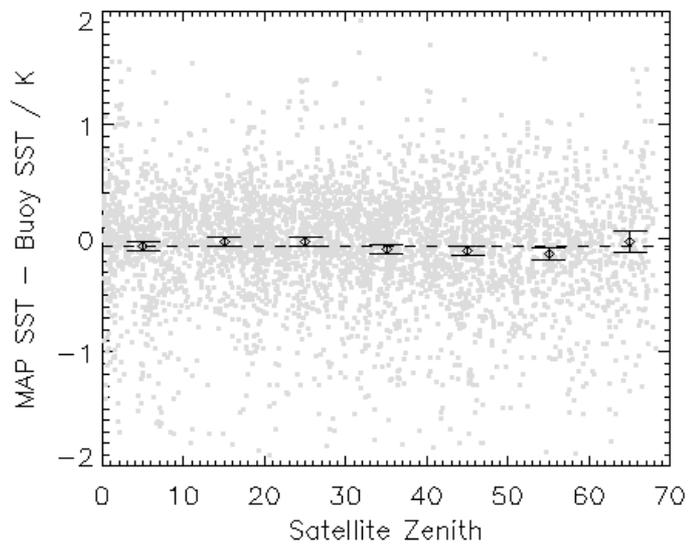
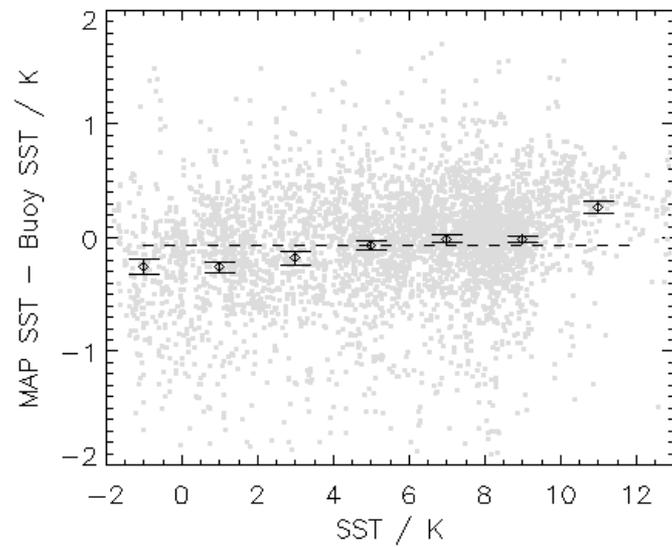
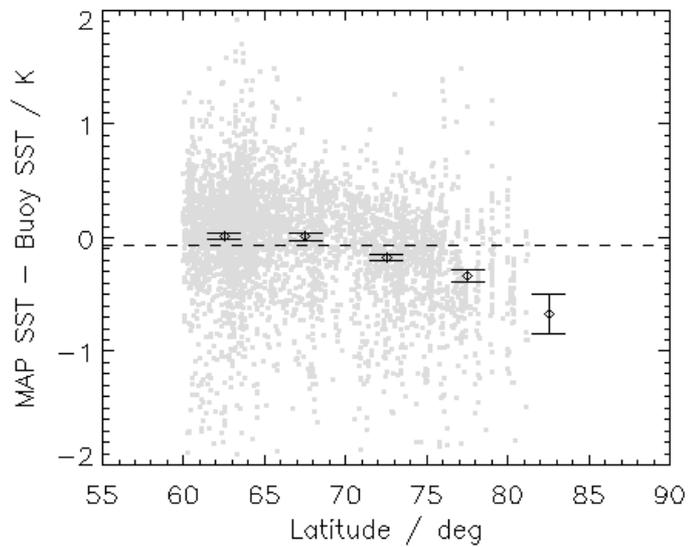
Median: -0.15 +/- RSD 0.49 K

ALL

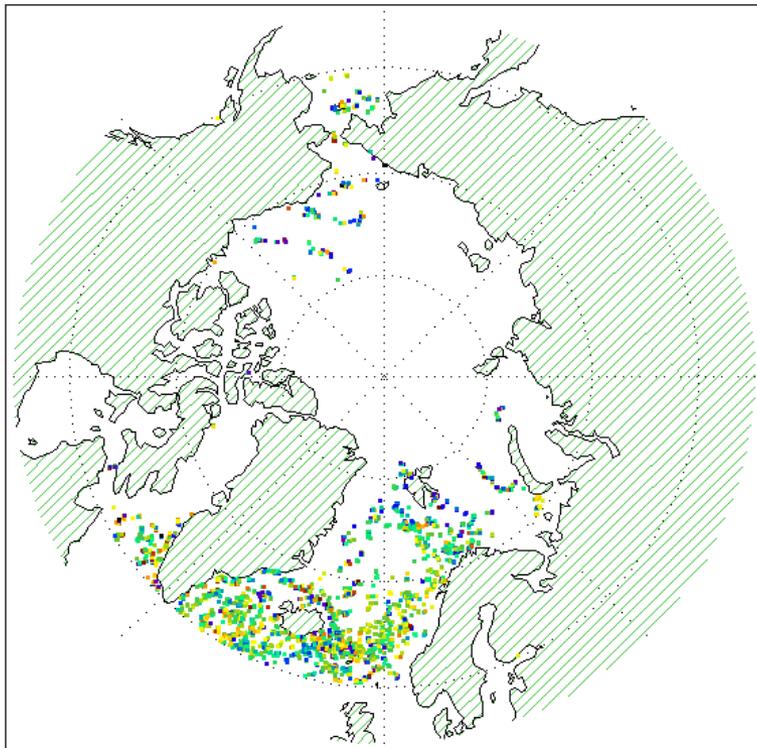
Mean: -0.07 +/- SD 0.58 K (4383)

Median: -0.01 +/- RSD 0.40 K





# Does using the BT adj help OE MAP?



-1.0      -0.5      0.0      0.5      1.0



MAPBC SST - Buoy SST / K

MAP, SAF bias correction

CL = 5

Mean:  $-0.01 \pm$  SD 0.48 K (1628)

Median:  $0.04 \pm$  RSD 0.36 K

CL = 4

Mean:  $-0.03 \pm$  SD 0.59 K (1708)

Median:  $0.03 \pm$  RSD 0.37 K

CL = 3

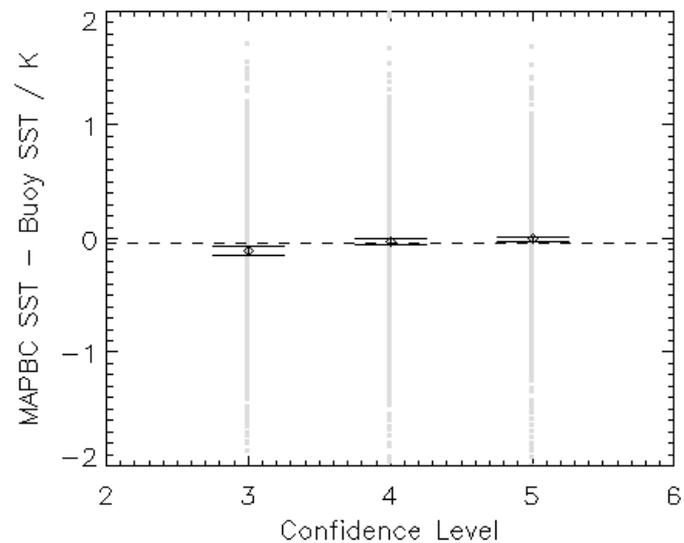
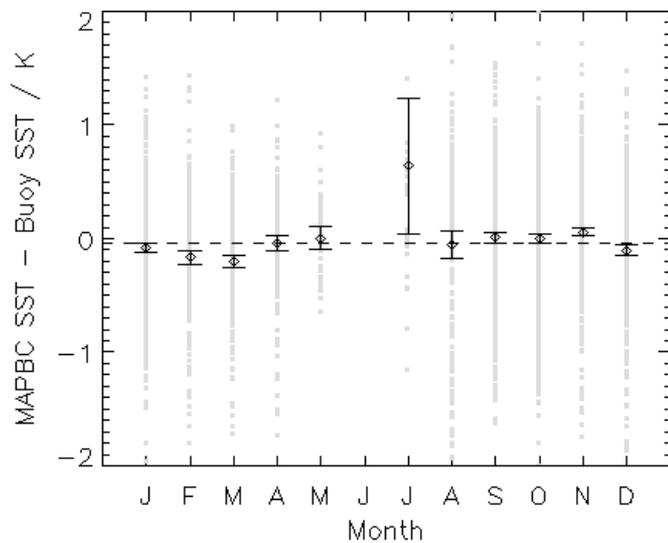
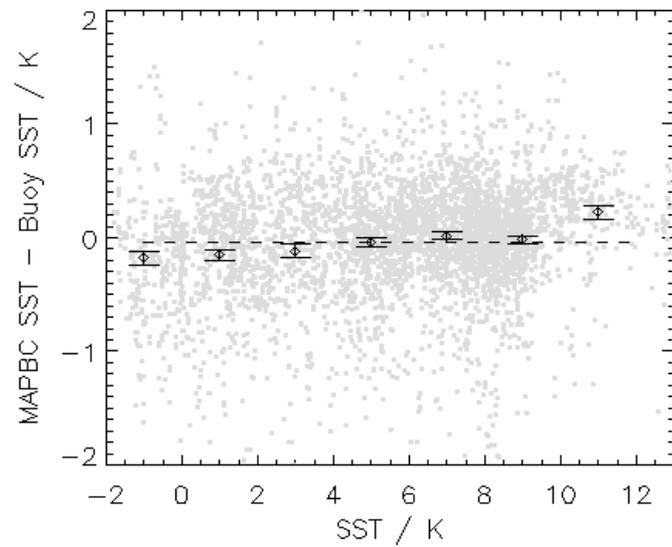
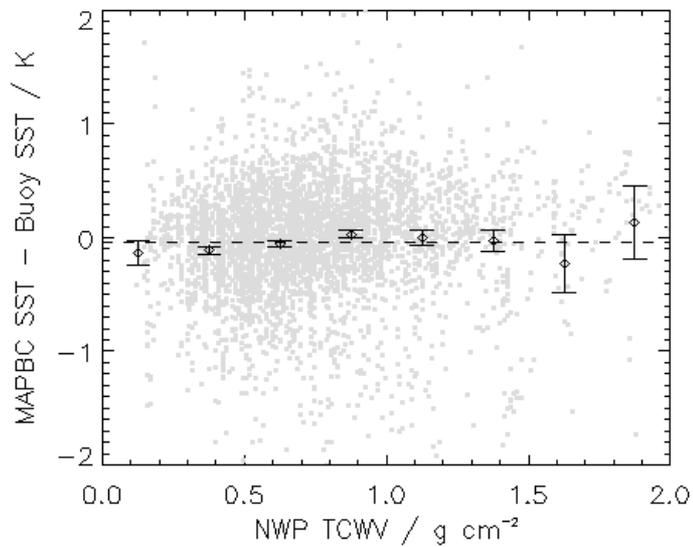
Mean:  $-0.11 \pm$  SD 0.69 K (1042)

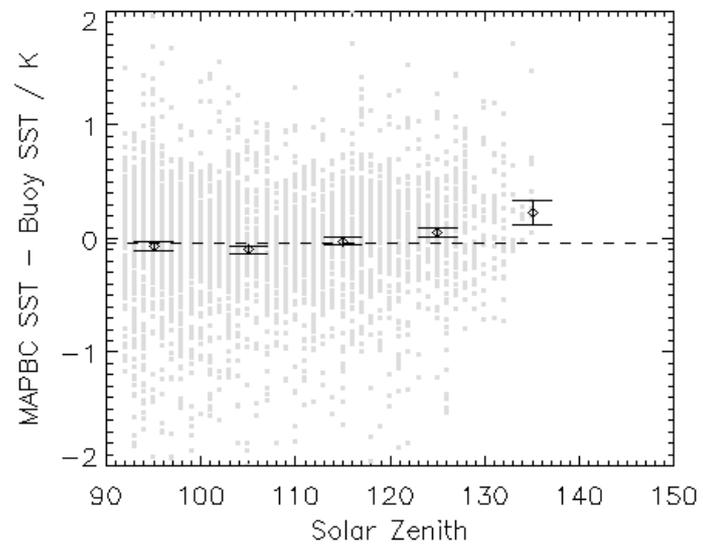
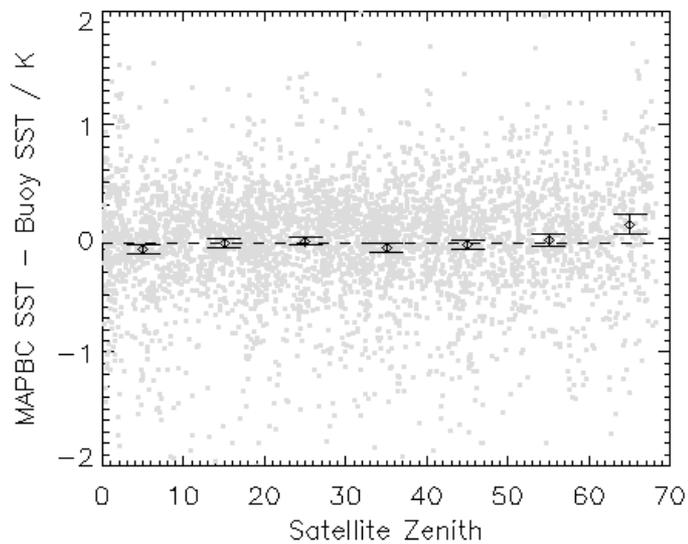
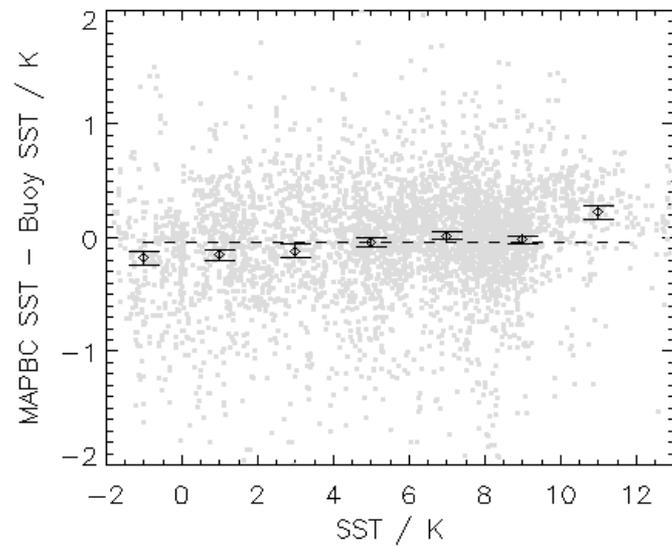
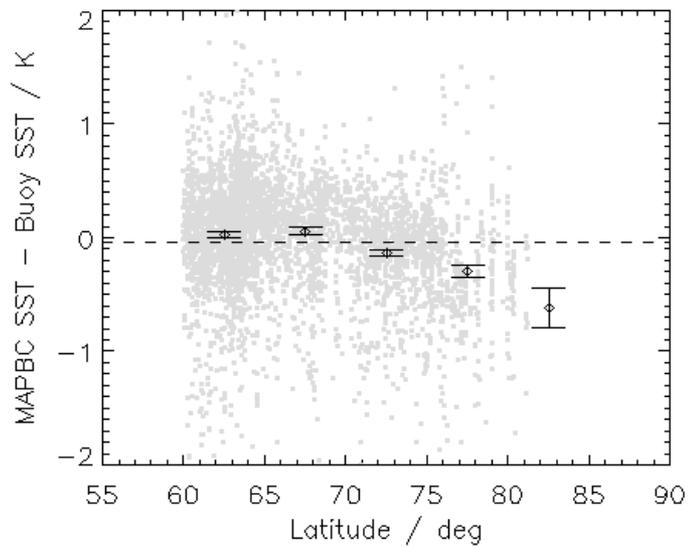
Median:  $-0.07 \pm$  RSD 0.49 K

ALL

Mean:  $-0.04 \pm$  SD 0.58 K (4378)

Median:  $0.02 \pm$  RSD 0.39 K





# Mid-point conclusions

- OSTIA small negative diffs overall (-0.14 K)
- Differences vary round year
- Op retrieval improved by using simulated bias correction, but negative diffs overall (-0.26 K)
- Varying differences round the year similar to OSTIA
  - Reflecting influence of Metop SSTs on OSTIA?
  - Moderated by use of simulated bias correction
  - Could near-surface stratification / strong winter skin effect between playing a role annual cycle of difference?
- OE relatively unbiased relative to drifters (-0.01 K)
- Varying differences round year damped in OE cf. OSTIA
- OE improved by SAF BT adjustment mainly for CL = 3
- All SSTs negatively biased cf. drifters at highest latitudes

# Ideas for bias-tolerant retrieval

- Modified Total Least Squares
  - Reported by Prabhat Koner at GHRSSST to need no BT bias correction for GOES-12 retrieval using 3.7, 11 and 13  $\mu\text{m}$
  - At same time OE without BC did badly
- Bias-aware Optimal Estimation
  - Empirical mean BT bias adjustment
  - Empirical forward model error covariance matrix, which reflects any correlated BT bias components

# Description of MTLs

- Like all similar methods, takes form of

$$\mathbf{x} - \mathbf{x}_b = \mathbf{G}(\mathbf{y} - \mathbf{f})$$

- In MTLs the gain  $\mathbf{G}$  is

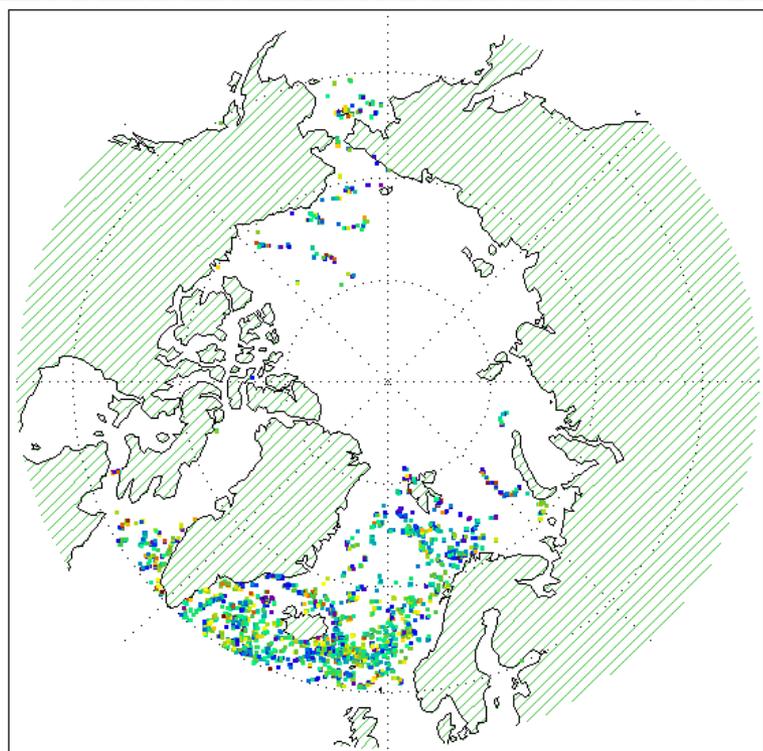
$$(\mathbf{K}^T \mathbf{K} + \lambda \mathbf{I})^{-1} \mathbf{K}^T$$

- The “clever” bit:
  - the regularisation parameter  $\lambda$  is variable
  - based on assessment of how much regularisation a particular inverse needs

# Deciding on $\lambda$

- The  $\mathbf{K}$  matrix contains  $d\mathbf{y}/dx$  and  $d\mathbf{y}/dw$  terms
- If  $\mathbf{y} - \mathbf{f}$  is close to a linear combination of columns of  $\mathbf{K}$  then  $\mathbf{y} - \mathbf{f}$  is plausibly explained by perturbations to  $x$  and  $w$ 
  - Therefore, the simulation is “good” and the observation error is “small” and the inverse needs minimal regularisation  $\rightarrow$  small  $\lambda$
- Otherwise, simulations and observations poorly match
  - the inverse should be strongly regularised  $\rightarrow$  large  $\lambda$
- The actual recipe of Prabhat is
  - Find eigenvalues of  $[\mathbf{K} \ \mathbf{y}-\mathbf{f}]$ , call these  $\mathbf{w}$
  - $\lambda = 2.\ln(\max(\mathbf{w})/\min(\mathbf{w})).\min(\mathbf{w})^2$
  - This form is apparently a choice based on experiment

# MTLS vs drifters



-1.0    -0.5    0.0    0.5    1.0



MTLS SST - Buoy SST / K

MTLS, no BT bias correction

CL = 5

Mean: 0.02 +/- SD 0.45 K (1629)

Median: 0.03 +/- RSD 0.37 K

CL = 4

Mean: -0.04 +/- SD 0.57 K (1710)

Median: 0.01 +/- RSD 0.36 K

CL = 3

Mean: -0.15 +/- SD 0.72 K (1044)

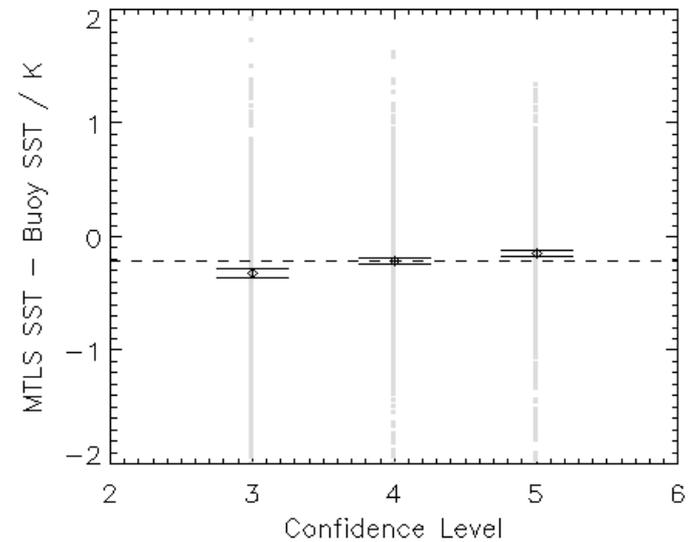
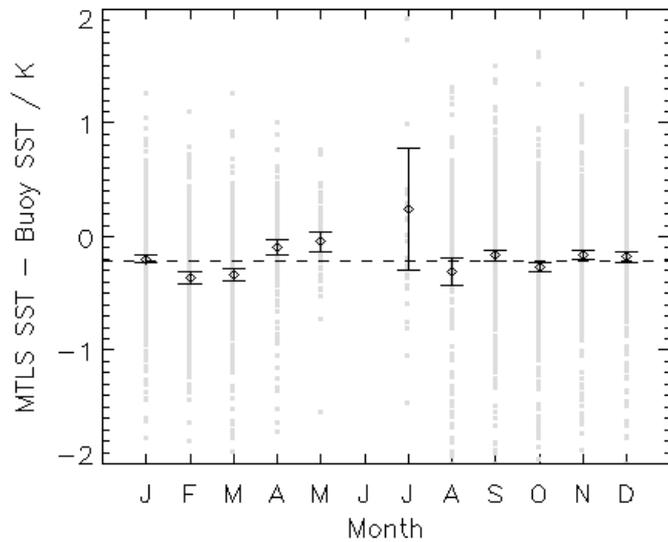
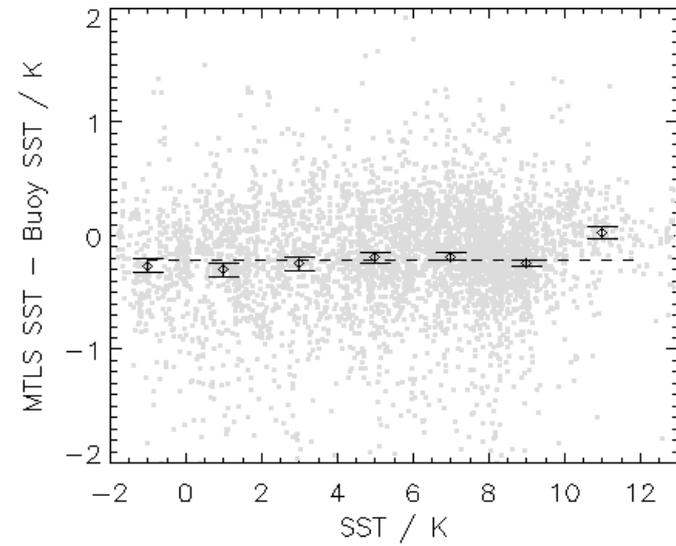
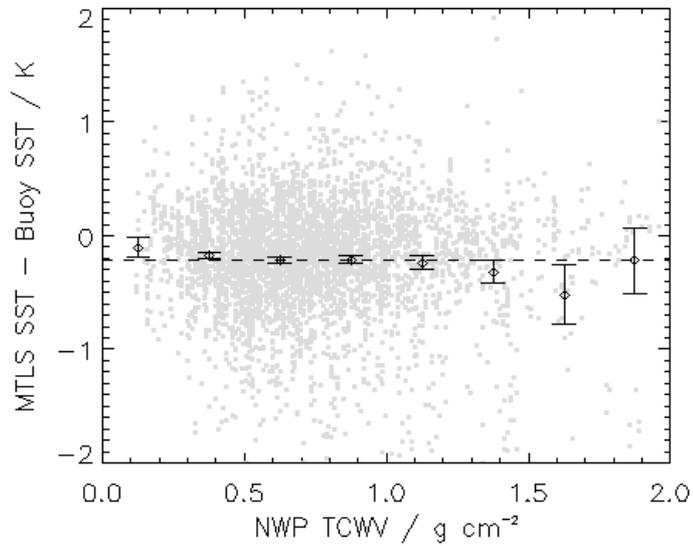
Median: -0.11 +/- RSD 0.51 K

ALL

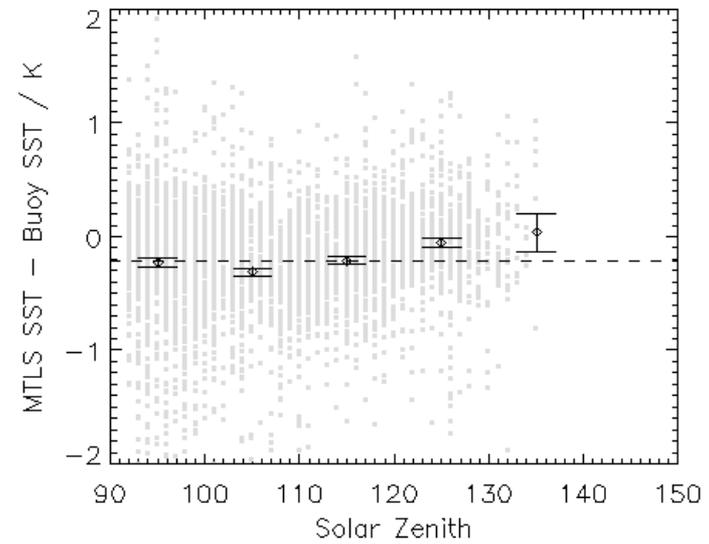
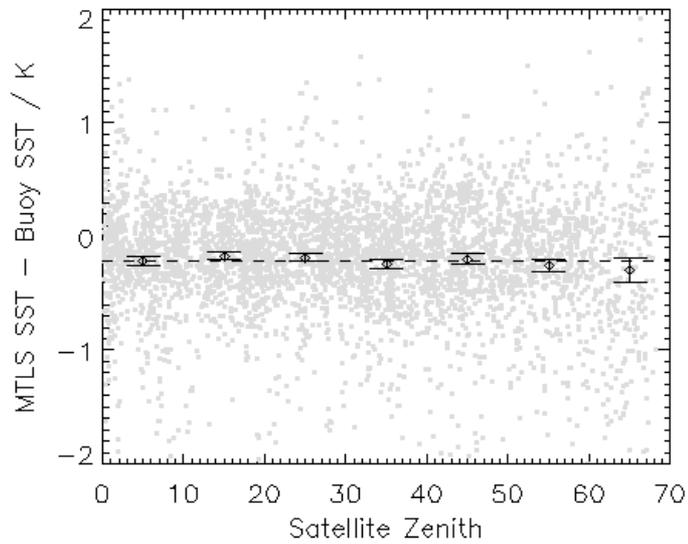
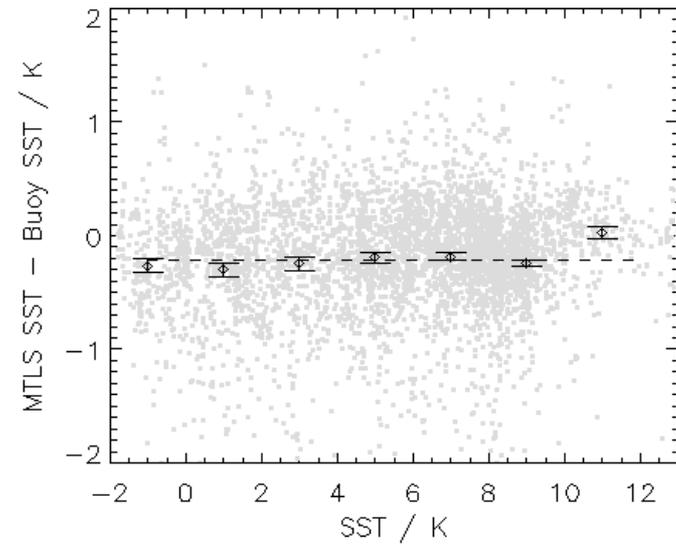
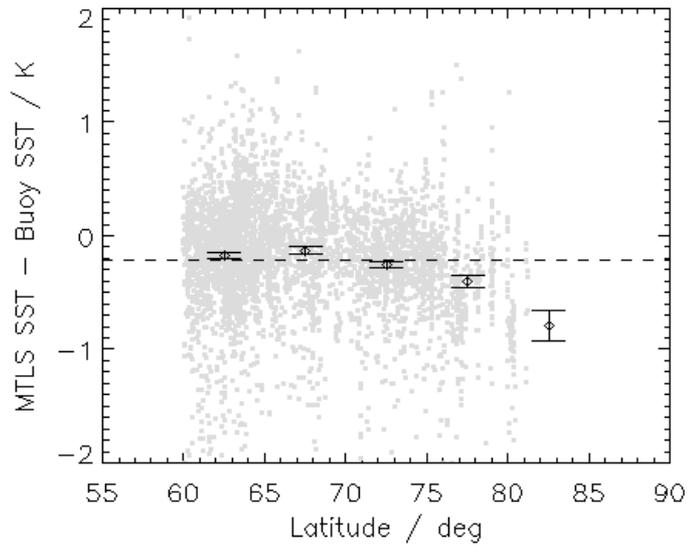
Mean: -0.04 +/- SD 0.58 K (4383)

Median: -0.00 +/- RSD 0.39 K

NB  
Figures  
done  
**without**  
adding  
0.17 K  
to  
account  
for skin



NB  
Figures  
done  
**without**  
adding  
0.17 K  
to  
account  
for skin



# The OE MAP gain matrix

- In normal OE the gain matrix can be written

$$\mathbf{S}_a \mathbf{K}^T (\mathbf{K} \mathbf{S}_a \mathbf{K}^T + \mathbf{S}_e)$$

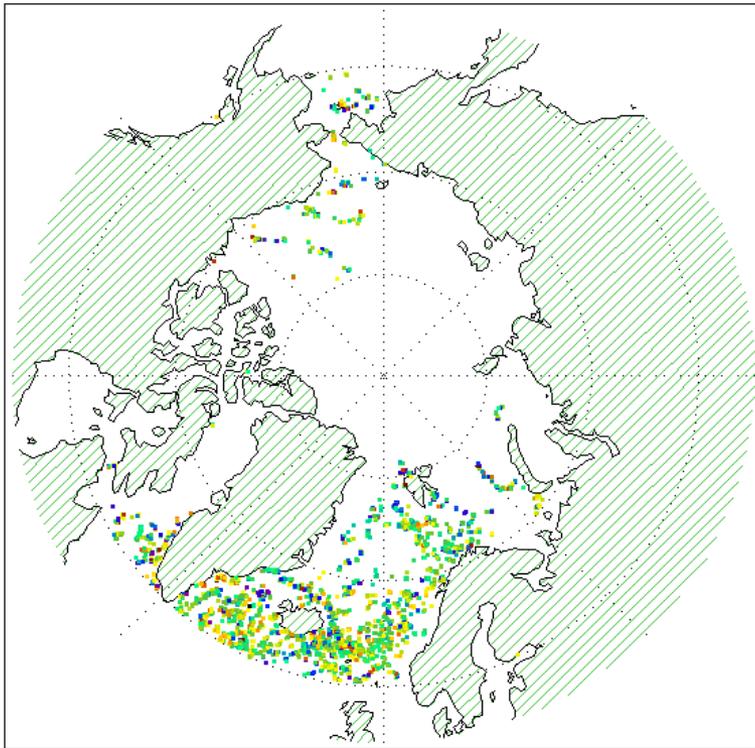
$\mathbf{S}_e$  represents noise plus forward model, both of which have been modelled simply as diagonals

$\mathbf{S}_a$  includes the prior SST error variance (which we think we know well) and the TCWV (which we don't know well)

# “Bias-aware” OE formulation

- First calculate mean  $\Delta \mathbf{f} = \mathbf{y} - \mathbf{f}$ 
  - accounting for skin effect when using OSTIA  $x_a$
  - stratified by CL, since varies systematically
- Then, find covariance( $\mathbf{y} - \mathbf{f} - \Delta \mathbf{f}$ )
- This should equal the mean of  $(\mathbf{K}\mathbf{S}_a\mathbf{K}^T + \mathbf{S}_e)$  but it doesn't because the error covariances are not well known
- Get a new estimate of  $\mathbf{S}_e$  as
$$\mathbf{S}_e^{BA} = \text{covariance}(\mathbf{y} - \mathbf{f} - \Delta \mathbf{f}) - \text{mean}(\mathbf{K}\mathbf{S}_a\mathbf{K}^T)$$
- This then estimates the correlated forward model or BT errors across the domain (plus real sensor noise)
- Retrieval is:  $x - x_a = \mathbf{S}_a\mathbf{K}^T(\mathbf{K}\mathbf{S}_a\mathbf{K}^T + \mathbf{S}_e^{BA})(\mathbf{y} - \mathbf{f} - \Delta \mathbf{f})$

# OE-BA vs. drifters



-1.0      -0.5      0.0      0.5      1.0



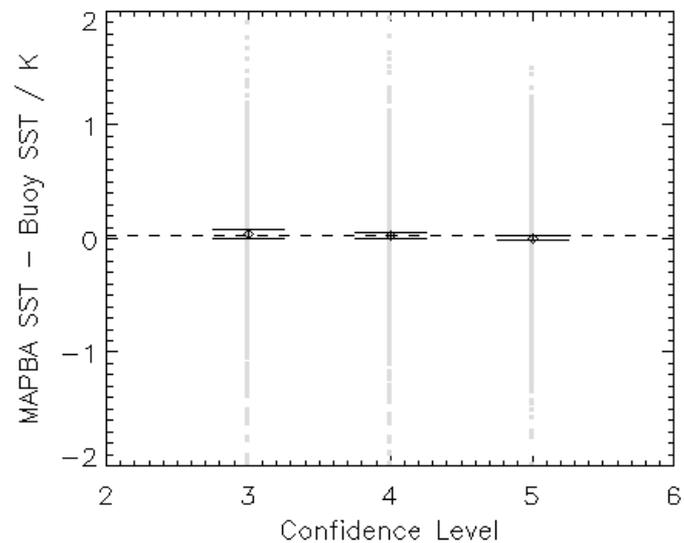
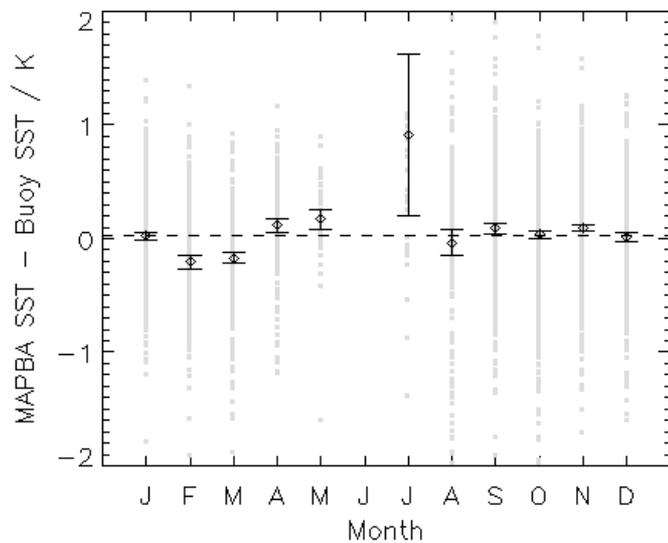
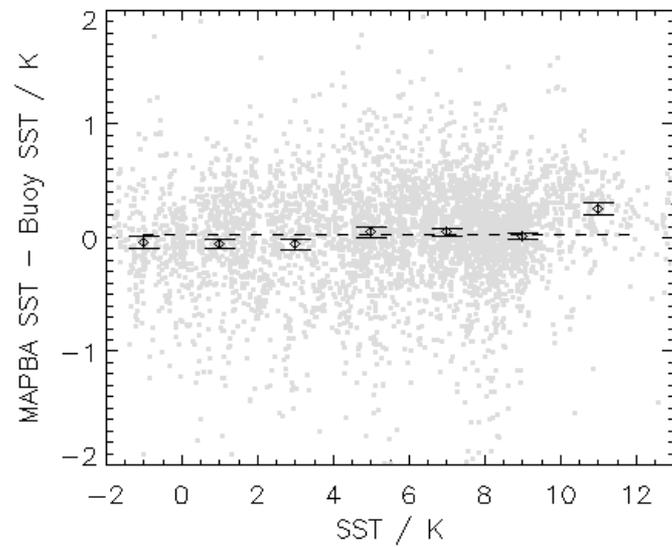
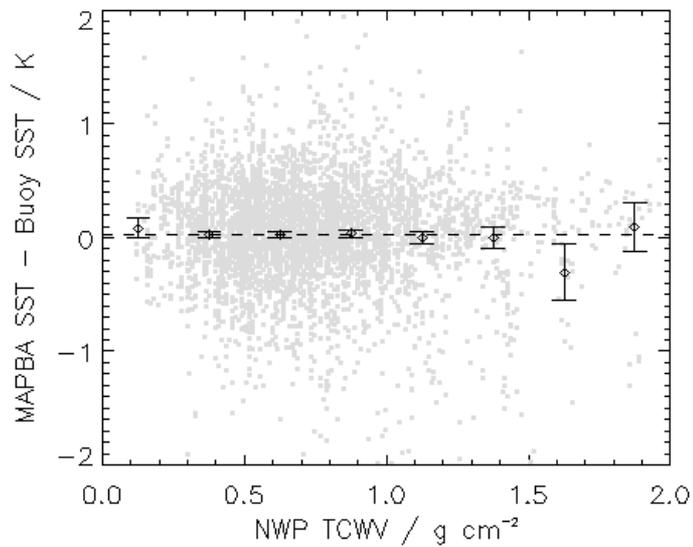
MAPBA SST - Buoy SST / K

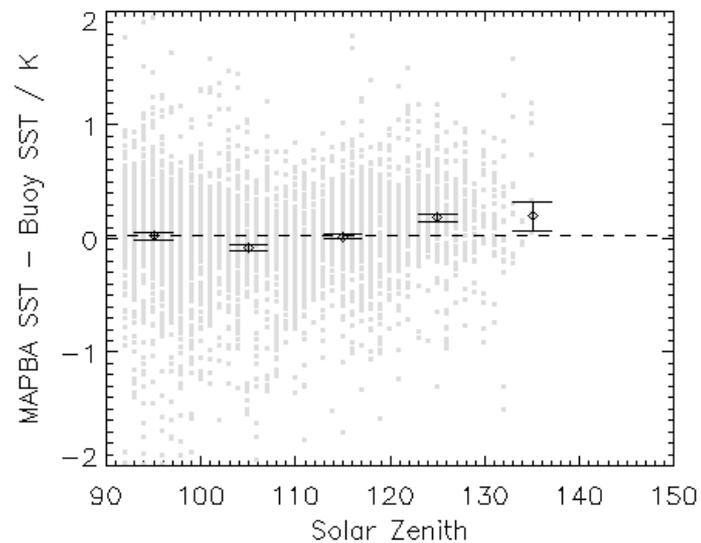
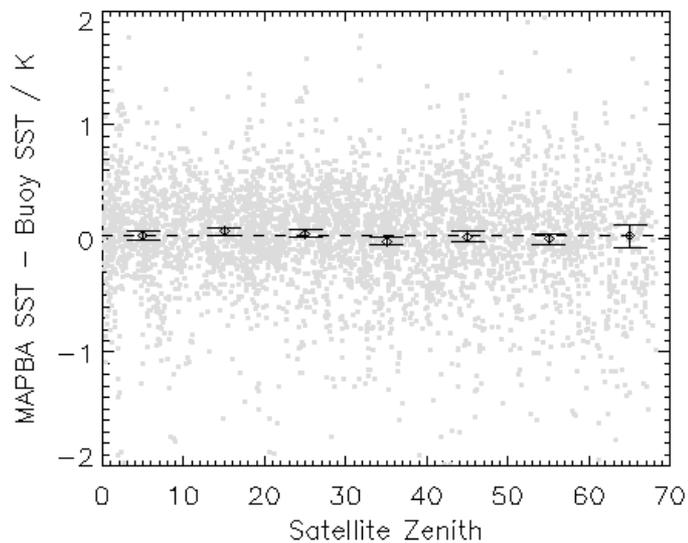
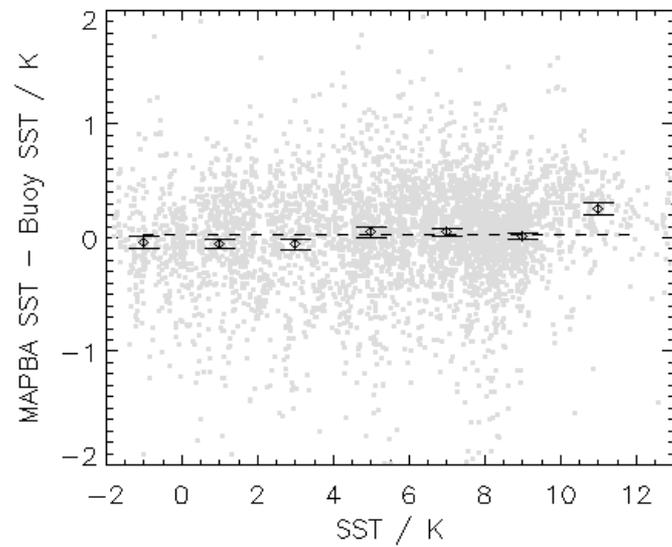
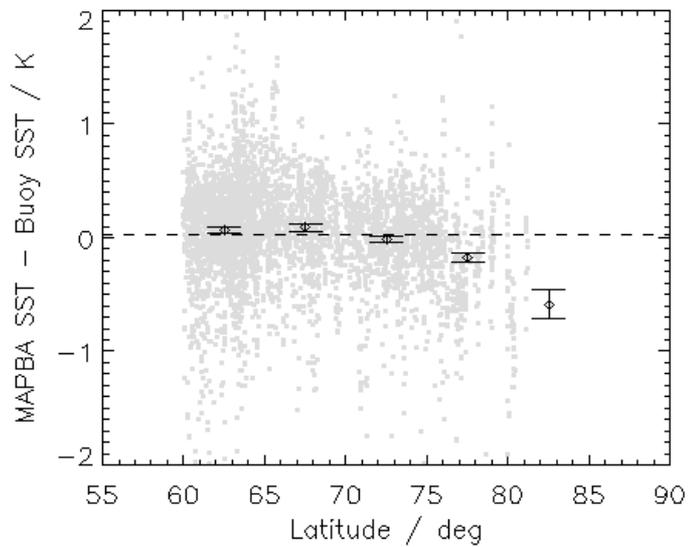
ALL

Mean: 0.02 +/- SD 0.53 K (4383)

Median: 0.05 +/- RSD 0.37 K

Reduction in SD!





# Conclusions on new methods

- MTLs performance similar to OE naive
  - $|\text{mean diff}| < 0.1 \text{ K}$
  - similar dispersion statistics
  - some functional biases improve, others degrade
- OE BA performance similar to OE BC
  - note CL biases flattened out
    - result of stratifying  $\Delta f$  by this variable
    - suggests strategy for attacking bias dependencies
  - seasonal variations not as good as OE BC
  - solar ZA and SST dependencies improved cf. OE BC

# Final remarks

- Bias-tolerant alternatives to BT adjustment scheme worth exploring further
  - But note: MTLs won't work for split window
  - Not sure if OE BA will work for split window
- All physics-based approaches seem to give different-but-similar-quality results
  - Coeffs + Sim Bias Corr (biased), OE BC, MTLs, OE BA
- Don't see in this data set any twilight problems using three channels
- Recommend adding calculated Fairall skin effect to MDs – skin effect variability may matter
  - Consider using skin estimate in forward model, retrieving skin explicitly (and adding skin estimate back to get subskin SST if required)